

# Bounding the number of affine roots using algebraic methods

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We consider multivariate polynomials over arbitrary fields, with a special interest in finite fields. We study the number of affine roots – with or without multiplicity. The methods used mainly rely on simple Gröbner basis theory. Besides being of general mathematical interest the results have several applications/implications in areas such as coding theory and function field theory.

## References

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